

# In-Flight Vicarious Calibration of High Spatial Resolution Remote Sensing Systems Using Specular Reflectors

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Evaluation Workshop  
March 18, 2009



Support provided  
by the NGA AGITK  
program

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# Outline

- Vicarious Calibration: A New Approach
- SPARC Method: A Unified Spatial and Radiometric Calibration Approach
- Spherical Mirrors as Radiometric Targets
- SPARC Design: Simplified Ground Truth Collection and Radiative Transfer Calculations
- Validation: SPARC applied to IKONOS



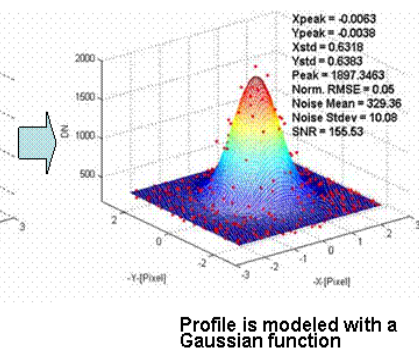
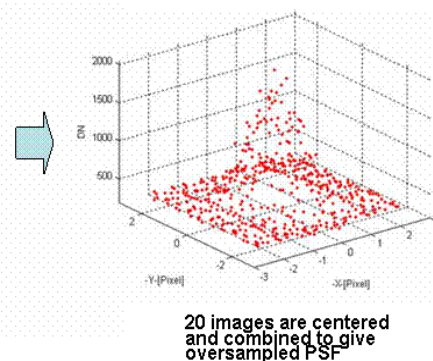
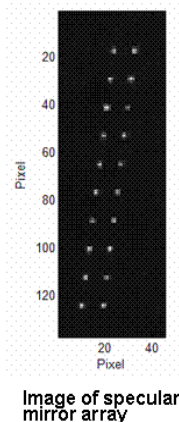
# A new Approach to Absolute Vicarious Calibration Using Spherical Reflectors

- Combines reflectance-based vicarious approach with stellar calibration
- Accomplished by creating an array of “solar stars” on the ground with convex spherical mirrors
- Each have well characterized radiometric properties and solar like spectra
- Targets are low cost, small and easy to deploy



## Previous Application of Convex Mirrors at South Dakota State University (SDSU)

- Used a grid of spherical reflectors to create point source images at different pixel phasing to oversample the sensor Point Spread Function (PSF)



- Purpose was for spatial analysis not radiometry



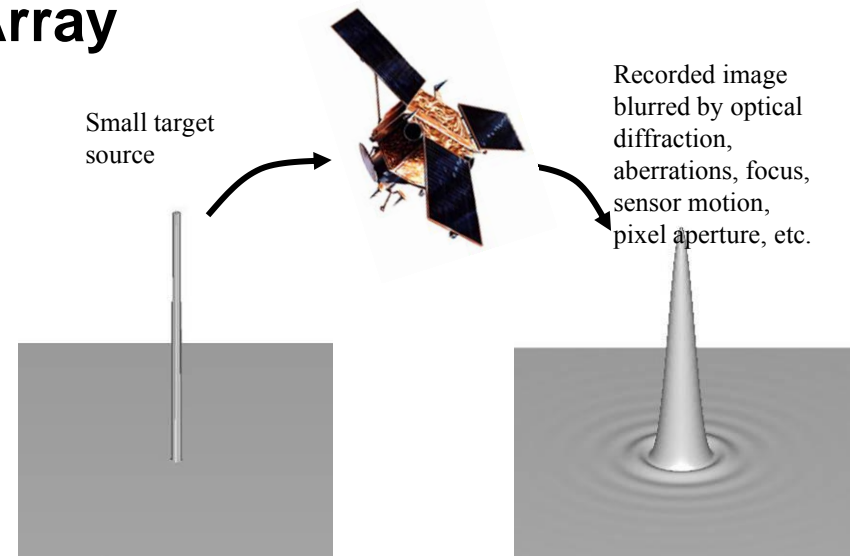
# SPecular Array Radiometric Calibration (SPARC) Method

US Patent Application No. 20100032557

Consists of two mirror arrays for spatial and radiometric calibration.

## Spatial Array

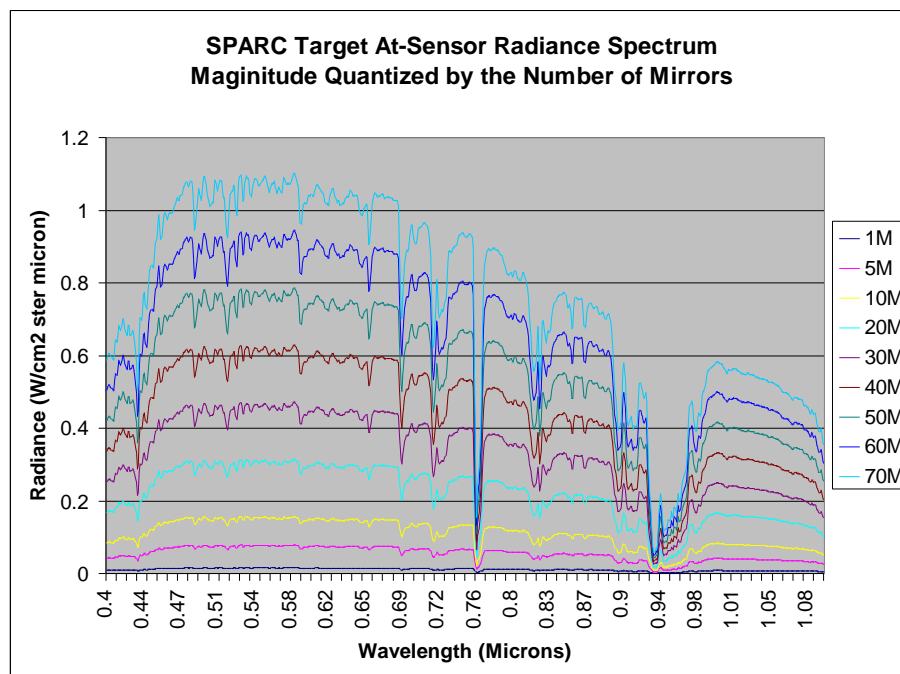
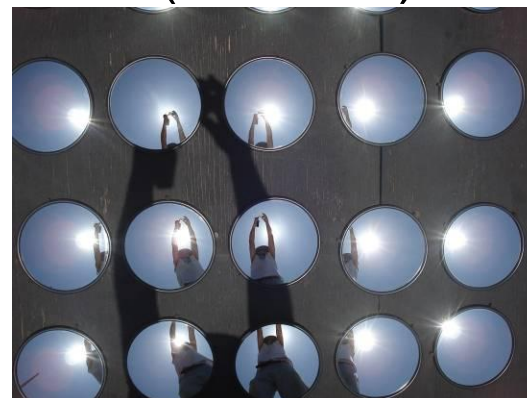
- Produces an oversampled estimate of the sensor point-spread-function (PSF)
- Modified version of SDSU method
- Purpose is to validate the PSF profile and provide knowledge of the ensquared energy when integrating image digital numbers (DN) within a limited spatial window around a small target
- Method takes advantage of the fact that all the energy originating from a subpixel target is contained in the volume of the PSF profile.



# Radiometric Array

## SPecular Array Radiometric Calibration (SPARC) Method

- SPARC uses panels of convex spherical mirrors to create a set of radiometric targets with different at-sensor radiance.
- Individual mirrors produce a virtual image of the sun with an upwelling intensity determined by the mirrors radius of curvature.
- Total intensity of each target is quantized by the number of mirrors.
- Design results in a simplified radiative transfer equation for calculating accurate values of at-sensor radiance.
- Only ground truth data required in the field for the calculation of at-sensor radiance is atmospheric transmittance.
- Reflectors for each target are spread over an area approximately the size of the sensors ground sample distance (GSD) or smaller (can be larger but not necessary).
- Targets are deployed on as dark and uniform a background as possible
- A SPARC array can be deployed in a couple hours



# Spherical Mirrors as Radiometric Targets

- Collimated light from the sun is reflected from a spherical surface nearly isotropically across the sky
- In a lossless medium the incident solar irradiance  $E_o(\lambda)$  can be shown to produce an upwelling intensity  $I(\lambda, \theta)$  by the relation

$$I(\lambda, \theta_i) = \frac{1}{4} \rho(\lambda, \theta_i) E_o(\lambda) R^2 = \text{watts/sr}$$

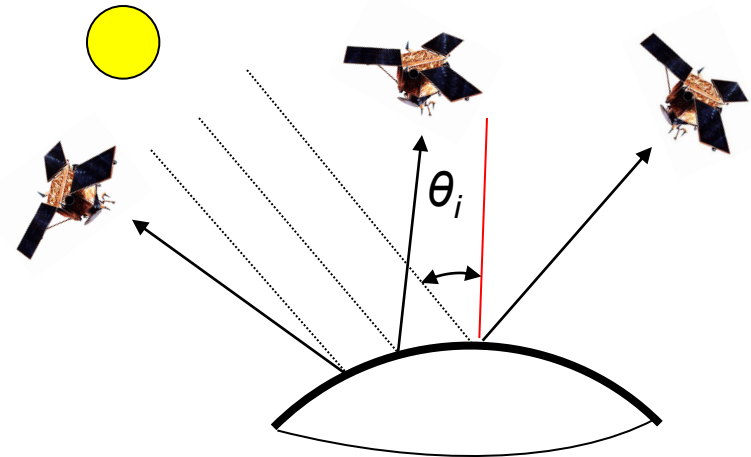
Where,

$\rho(\lambda, \theta_i)$  = Specular reflectance

$R$  = Mirror radius of curvature

$\theta_i$  = Angle of incidence (AOI) relative to surface normal

- Variation in upwelling intensity of reflected natural light is typically only a few percent over the hemispherical sky



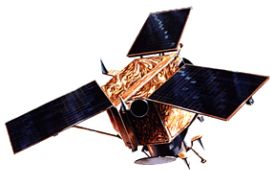
• **Bidirectional Reflectance Distribution Function** (BRDF) effects are small and accurately characterized in the laboratory

• The are no surface foreshortening effects

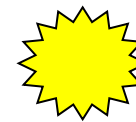
• Upwelling intensity is independent of mirror orientation



Intensity is controlled accurately by simply changing the radius of curvature



$$I_1 \gg I_2 \gg I_3$$

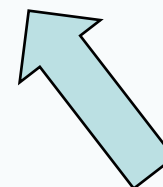


Array can stimulate sensor over the entire dynamic range (through saturation).

$$I_1 \propto R_1^2$$

$$I_1 \propto R_2^2$$

$$I_1 \propto R_3^2$$



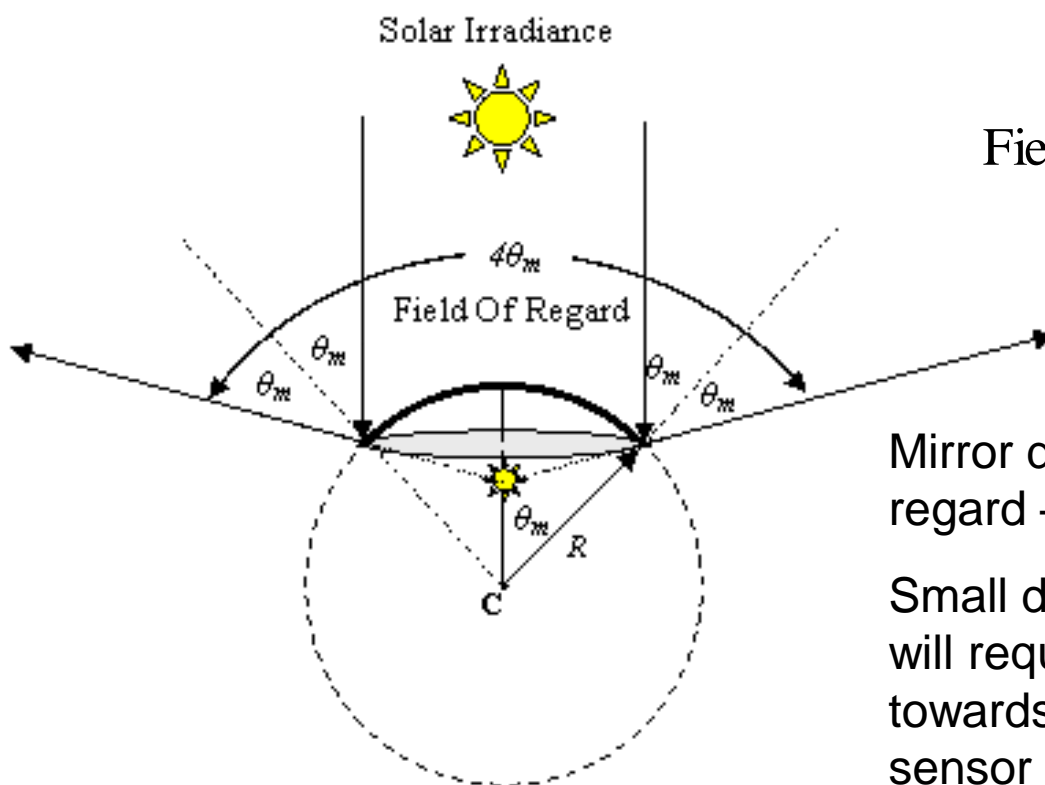
$$R_1 \gg R_2 \gg R_3$$



# Solid Angle Of Reflected Mirror Intensity (Field-Of-Regard)

Extent of the field-of-regard is determined by the diameter of the mirror (W)

$$\text{Field - of - Regard} = 4 \arcsin\left(\frac{W}{2R}\right)$$



Mirror diameter only affects the field of regard – not intensity

Small diameter mirrors can be used but will require alignment of the optical axis towards the midpoint between sun and sensor

# Only Atmospheric Transmittance Drives Radiative Transfer Calculations

Low spatial frequency sources add to small target signal as a uniform background



$E_o$  – Top-of-atmosphere solar spectral irradiance

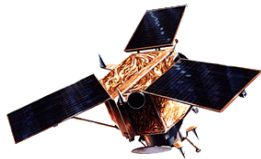
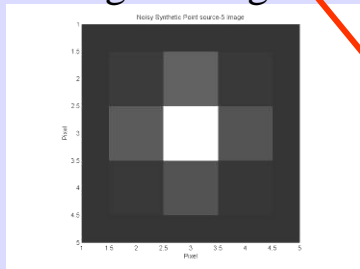


Image of target



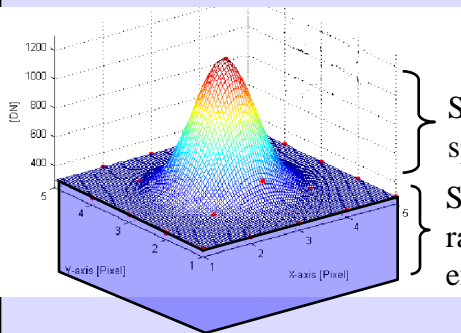
$T_1$  – Sun to target transmittance

$T_2$  – Target to sensor transmittance

At-sensor intensity

$$I_{at-sensor} \propto \rho T_1 T_2 E_o$$

$\rho$  – Specular Reflectance



Signal from specular target

Signal from sky path radiance, adjacency effect, stray light, etc.

Target signal is elevated above background (Surface background radiance, sky path radiance, adjacency effect, stray light, etc.) and separable – Background becomes a bias and is subtracted out based on image data alone

# No need to “walk the site”

- Ground truth reflectance measurements are not needed!!
- No need for a field spectrometer (ASD)
- Mirror reflectance is measured in the laboratory (>5x more accurate than diffuse reflectance)
- Target reflectance uncertainty becomes negligible
- All measurements become instantaneous.
- Reflectance temporal variability issues go away when comparing data from different collects





# SPARC Radiative Transfer Equation For Effective TOA Radiance

## TOA Intensity

$$I(\lambda, \theta_r) = \frac{1}{4} \rho(\lambda, \theta_i) T_1(\lambda) T_2(\lambda) E_o(\lambda) R^2 \quad \text{watts/(sr micron)}$$

## TOA Radiance/Mirror

$$L_{TOA}(\lambda, \theta_r) = \frac{\rho(\lambda, \theta_i) T_1(\lambda) T_2(\lambda) E_o(\lambda)}{\Omega_{IFOV}} \left( \frac{R}{2H} \right)^2 = \rho(\lambda, \theta_i) T_1(\lambda) T_2(\lambda) E_o(\lambda) \left( \frac{R}{2GSD} \right)^2$$

$\rho(\lambda, \theta_i)$  = specular reflectance

Watts/(m<sup>2</sup> sr micron)/mirror

$T_1(\lambda)$  = Sun to ground transmittance

Uncertainty is dominated by the transmittance which is directly defined by the uncertainty in the calibration of the sunphotometer (all other terms are < 1%)

$T_2(\lambda)$  = Ground to sensor transmittance

$E_o(\lambda)$  = Solar spectral constant

$$\sigma_{L_{TOA}}(\lambda) \approx 2 \cdot \sigma_T(\lambda) \approx 2 \cdot \sigma_{lo}(k)$$

$R$  = Mirror radius of curvature (m)

$H$  = Sensor-to-mirror distance (m)

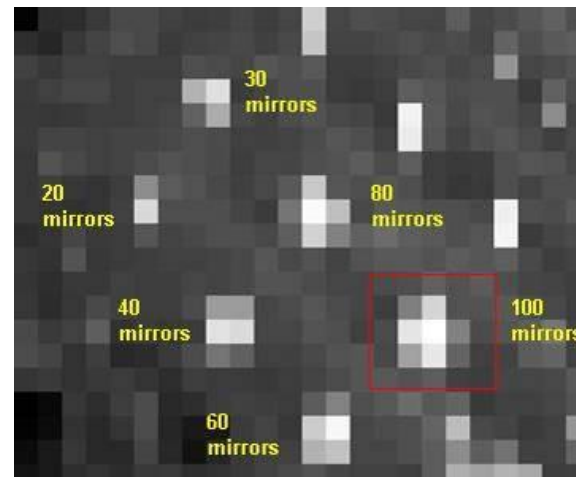
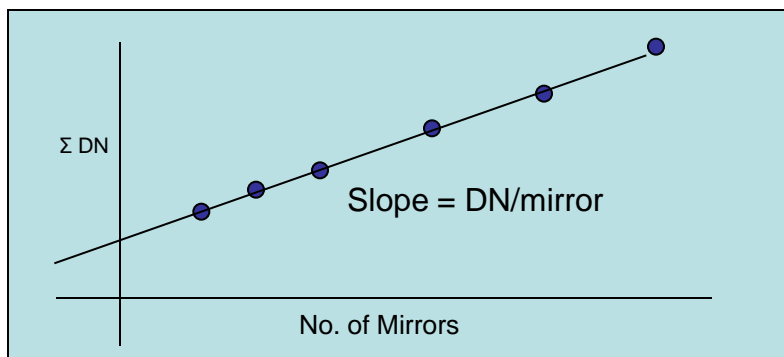
Where  $lo(k)$  is the TOA relative solar spectral response in sunphotometer band  $k$

$\Omega_{IFOV}$  = Projected solid angle of single detector on the ground

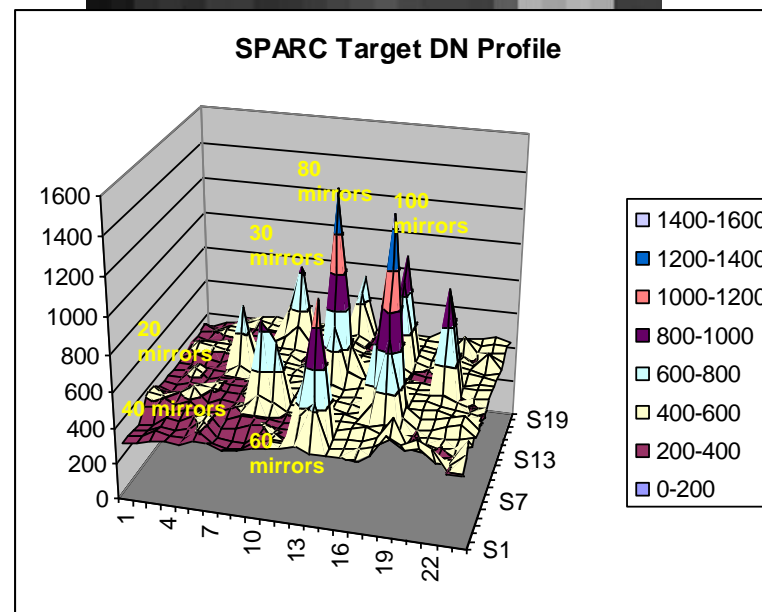
$GSD$  = Ground Sample Distance (m)

# SPARC Target Image Analysis

- Simply measure the sensor response ( $\Sigma$  DN) of a set of SPARC targets having different effective radiance
- Processing consists of equalization of detector response but no resampling
- A square window is centered on each target and the DN values are summed. (Red box)
- Plot  $\Sigma$  DN vs. No. of mirrors to get DN/Mirror from the slope.
- If background is sufficiently uniform, in principle, no background analysis is necessary (Background affects the bias not the slope)



IKONOS  
Green  
Band  
Image







# SPARC Based Absolute Gain Coefficient Calculation

$$\text{CalCoef}(\lambda) = \frac{\text{DN} / \text{Mirror}(\lambda)}{\text{Radiance} / \text{Mirror}(\lambda) \cdot \text{Bandwidth}(\lambda) \cdot \text{EnsEnergyCor}} = \text{DN} / (\text{Watts} / \text{m}^2 \text{sr})$$

$$\text{Radiance} / \text{Mirror}(\lambda) = \frac{\sum [L_{\text{TOA}}(\lambda, \theta_r) \cdot \text{RSR}(\lambda)]}{\sum \text{RSR}(\lambda)} = \text{Band integrated radiance [Watts/(m}^2 \text{sr)]/mirror}$$

$\text{DN} / \text{Mirror}(\lambda) =$  slope of  $\Sigma \text{DN}$  vs. No. of mirrors measured from the SPARC target response profiles.

$\text{Bandwidth}(\lambda) =$  Bandwidth of spectral band  $\lambda$  ( $\mu\text{m}$ )

$\text{EnsEnergyCor} =$  Estimated fraction of ensquared energy contained within the applied SPARC target response profile integration window ( $\approx 1$ ).

Corrects for energy lost in the wings of the PSF outside the DN/Mirror measurement window. Size of window depends on target separation practical for the ground site and background uniformity.



# SPARC Method Applied to the Absolute Calibration of IKONOS

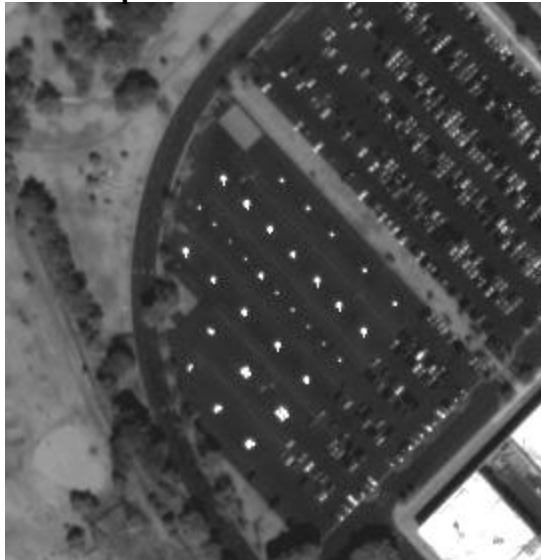
- On Sept 10, 2009, IKONOS images were collected of SPARC spatial and radiometric reflectors
- Site: Parking lot of Raytheon SAS Facility in El Segundo, CA.
- Two miles south of the LAX airport
- Elevation 35 m
- Three images were collected in a single overpass
- One recorded outside the field of regard to reveal detailed background levels (Limiting the width of the field-of-regard allows the scene to be viewed with the sun turned off!)
- For validation purposes number of targets is an overkill. In principle, only 4 to 6 SPARC targets are needed for radiometric calibration.





# Sept 10, 2009 IKONOS Images

po\_365282



po\_365283



po\_365284



Acquired Nominal GSD  
Pan Cross Scan: 0.91 meters  
Pan Along Scan: 0.87 meters  
MS Cross Scan: 3.64 meters  
MS Along Scan: 3.49 meters  
Scan Azimuth: 180.01 degrees  
Scan Direction: Reverse  
Nominal Collection Azimuth: 66.7620 degrees  
Nominal Collection Elevation: 70.34628 degrees  
Sun Angle Azimuth: 146.0466 degrees  
Sun Angle Elevation: 56.37735 degrees

Acquired Nominal GSD  
Pan Cross Scan: 0.88 meters  
Pan Along Scan: 0.85 meters  
MS Cross Scan: 3.53 meters  
MS Along Scan: 3.41 meters  
Scan Azimuth: 180.01 degrees  
Scan Direction: Reverse  
Nominal Collection Azimuth: 106.6828 degrees  
Nominal Collection Elevation: 73.68076 degrees  
Sun Angle Azimuth: 146.1832 degrees  
Sun Angle Elevation: 56.41706 degrees

Acquired Nominal GSD  
Pan Cross Scan: 0.92 meters  
Pan Along Scan: 0.99 meters  
MS Cross Scan: 3.68 meters  
MS Along Scan: 3.94 meters  
Scan Azimuth: 0.01 degrees  
Scan Direction: Forward  
Nominal Collection Azimuth: 155.0008 degrees  
Nominal Collection Elevation: 63.96876 degrees  
Sun Angle Azimuth: 146.4022 degrees  
Sun Angle Elevation: 56.48040 degrees

Images have limited processing – flat field response equalization but no resampling

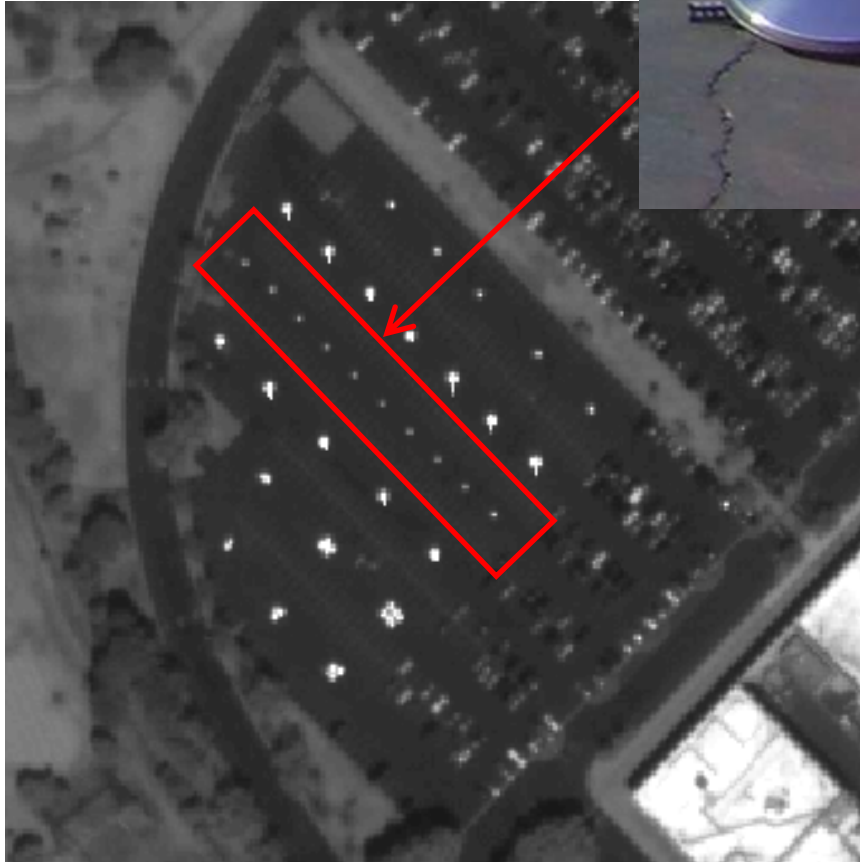
16



# Spatial Analysis

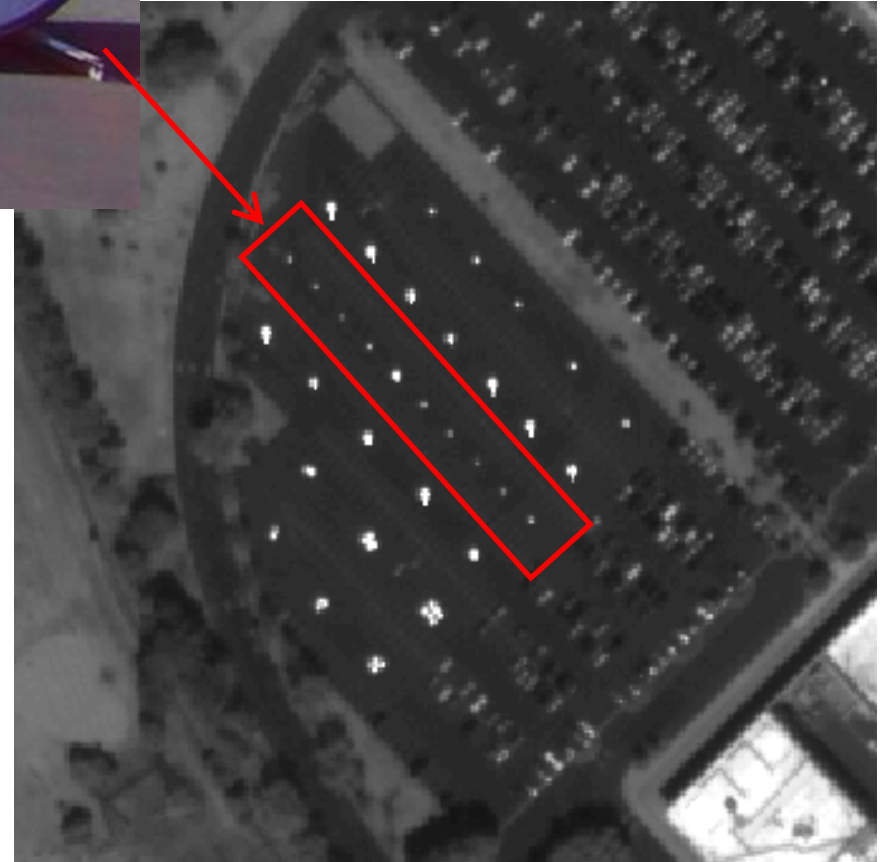
Mirror Array for Pan Band  
PSF FWHM measurements

po\_365282



20" diameter stainless steel  
convex mirror,  $R = 1.25$  m

po\_365283

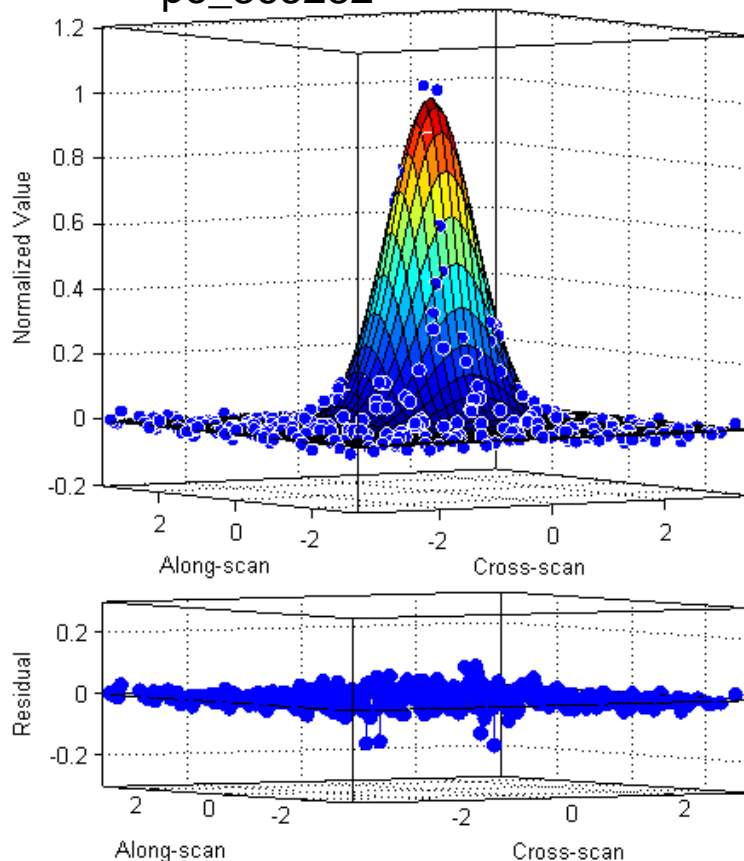






# Pan Band PSF FWHM Measurement

po\_365282



Percent RMSE = 3.3%

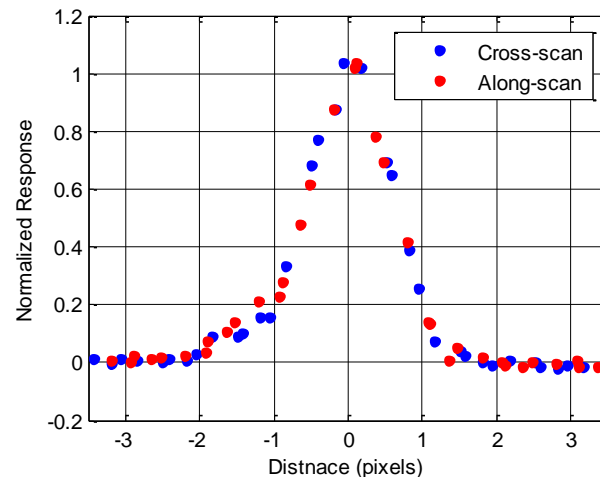
 $R^2$  Coefficient of Determination = 0.96

Image po\_365282

Cross-scan FWHM

1.27 0.04 pixels

Along-scan FWHM

1.34 0.03 pixels

Image po\_365283

Cross-scan FWHM

1.27 0.04 pixels

Along-scan FWHM

1.32 0.04 pixels

Multispectral detector pitch is 4x larger.

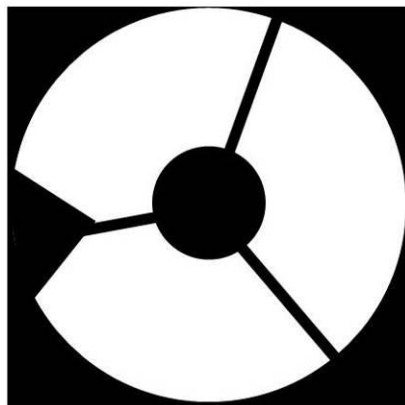
Implies multi-spectral FWHM  $\approx 0.3$  pixels (Band Dependent)

Confirms optical system can be modeled as roughly diffraction limited with nominal aberrations





# Ensquared Energy Calculations

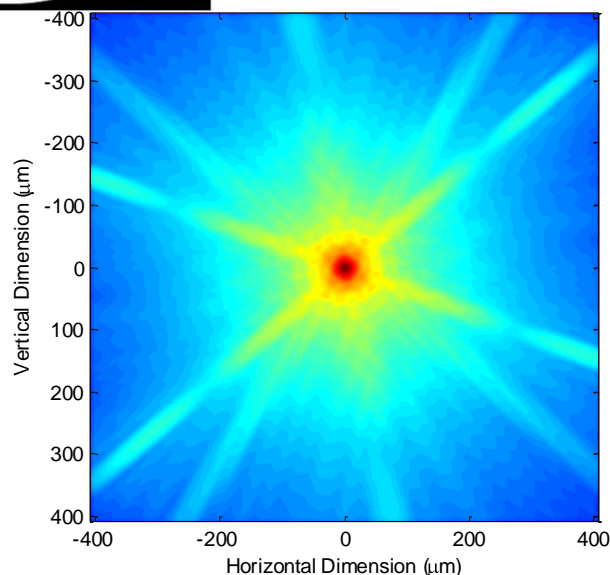


Polychromatic  
PSF from pupil  
mask and  
preflight  
interferogram  
based model

Green

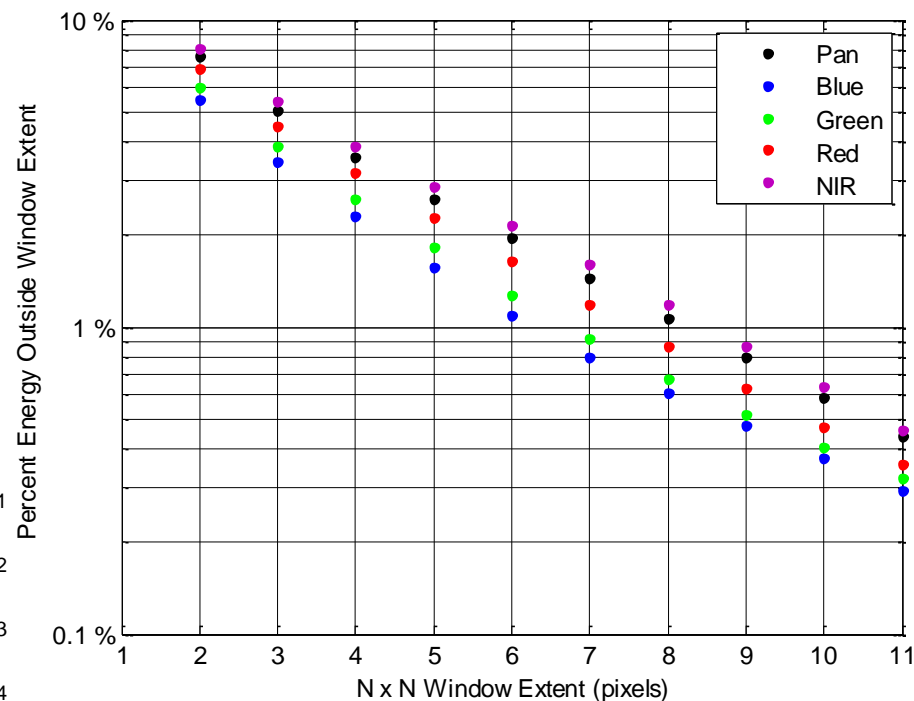
IKONOS Pupil  
Mask

Log  
Scale



Pixels are 48  $\mu\text{m}$  square MSI band  
detector elements

Results are accurate to  $\sim 0.5\%$



Multispectral Band	Blue	Green	Red	NIR
<b>EnsqEnergyCor</b> (3x3 pixels)	0.968	0.962	0.958	0.948

Image analysis of SPARC target background  
will be based on a 3 x 3 pixel window  
(based on separation between targets in MS images)

# Radiometric Analysis

- Atmospheric transmittance was measured with a shadowband radiometer.
- Aerosol extinction was derived and used to constrain MODTRAN model of atmospheric transmittance



**MFRSR\*** Atmospheric Measurements for Sept. 10, 2009 IKONOS Overpass at 18:39 UTC.

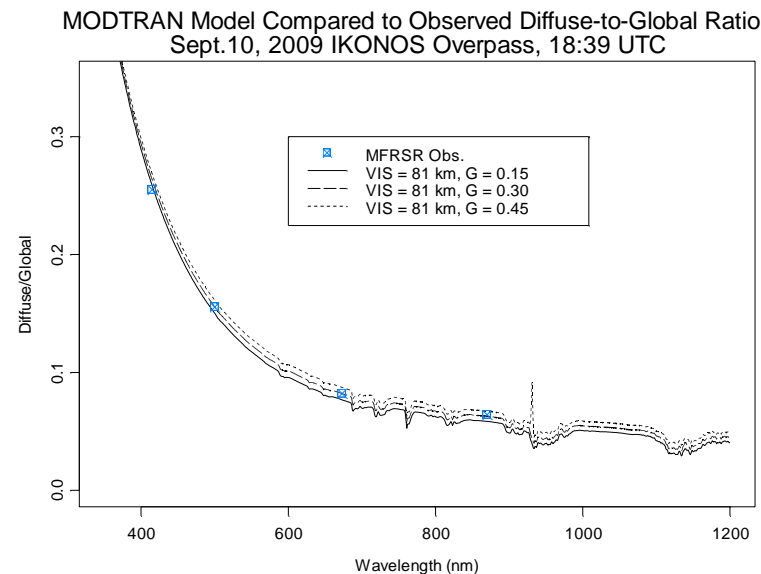
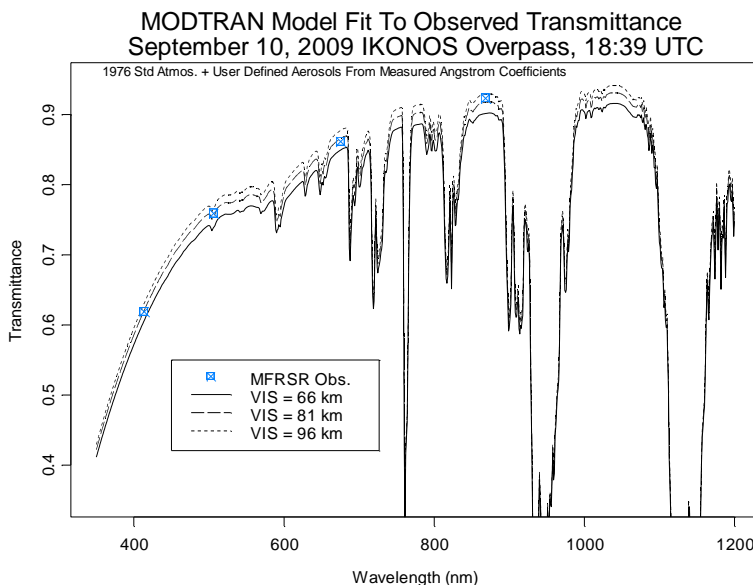
MFRSR Spectral Band Center (nm)	413.9	506.2	675.5	868.5
Transmittance Calibration Uncertainty (% 1 Sigma)	2.6	2.3	2.0	1.5
Sun to Ground Atmospheric Transmittance	0.619	0.759	0.861	0.923
Diffuse-to-Global Ratio	0.255	0.155	0.082	0.064

Uncertainty based on ~ 30 Langley plots recorded at the target site

\*Multi-Filter Rotating Shadowband Radiometer

# Transmittance Spectrum Calculated with MODTRAN\*

- Visibility parameter was adjusted to reproduce the observed transmittance and diffuse-to-global ratio at the time of the overpass



Minimum residuals were achieved (<2%) with VIS = 81 km

Agreement with diffuse-to-global ratio (relative measurement) provides independent confirmation that the sunphotometer was correctly calibrated.

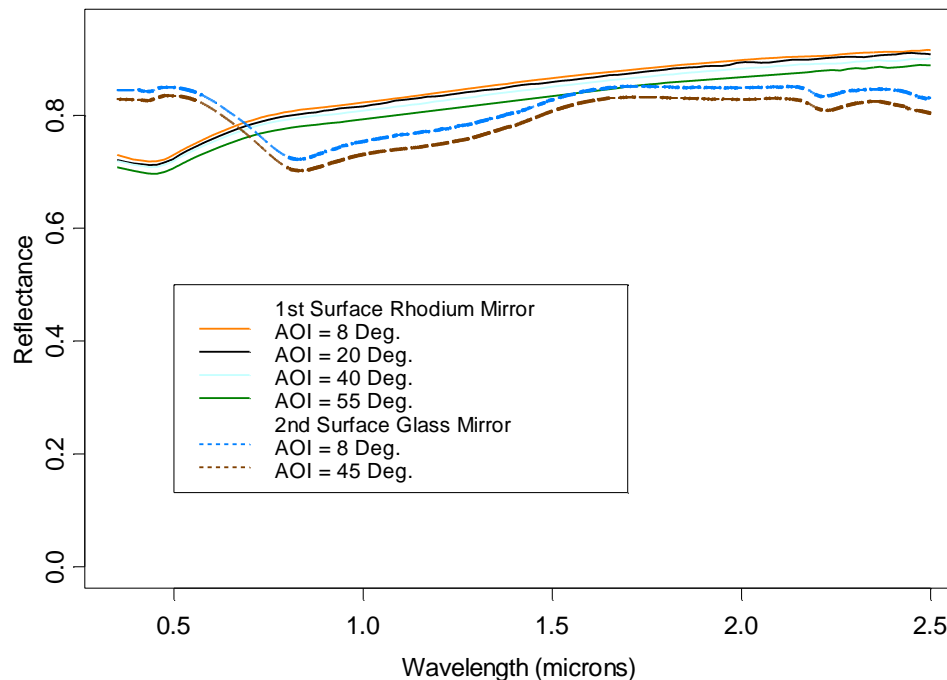
\*MODerate resolution atmospheric TRANsmission

# Mirror Reflectance Spectrum: Measured with a Laboratory Reflectometer

- Mirrors deployed on asphalt parking lot
- 2<sup>nd</sup> surface aluminized glass mirrors (D.O.T. approved truck mirrors with R = 18 inches)



Mirror Reflectance Variation With Angle Of Incidence



- Reflection is high, spectrally flat and varies slightly with angle of incidence (AOI)

• Reflectance knowledge accuracy ~0.25% VNIR and ~0.5% SWIR (1 sigma)

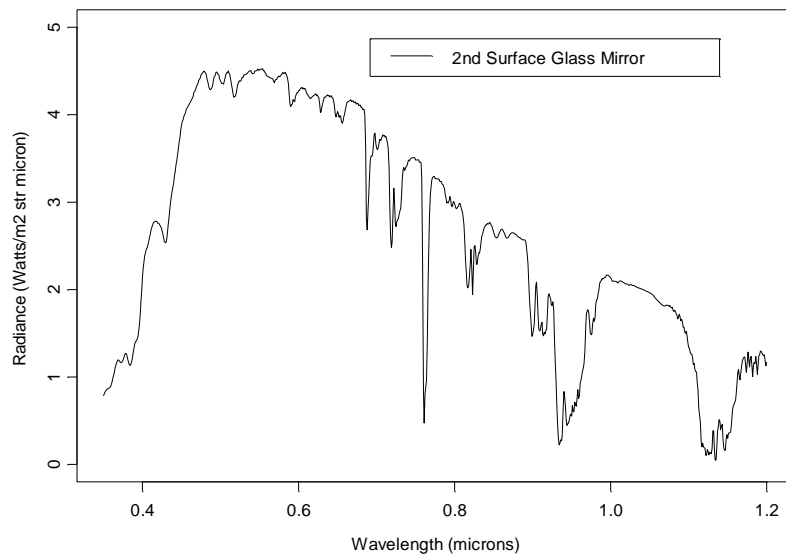
• Slight variation corrected by interpolation based on AOI for each collect



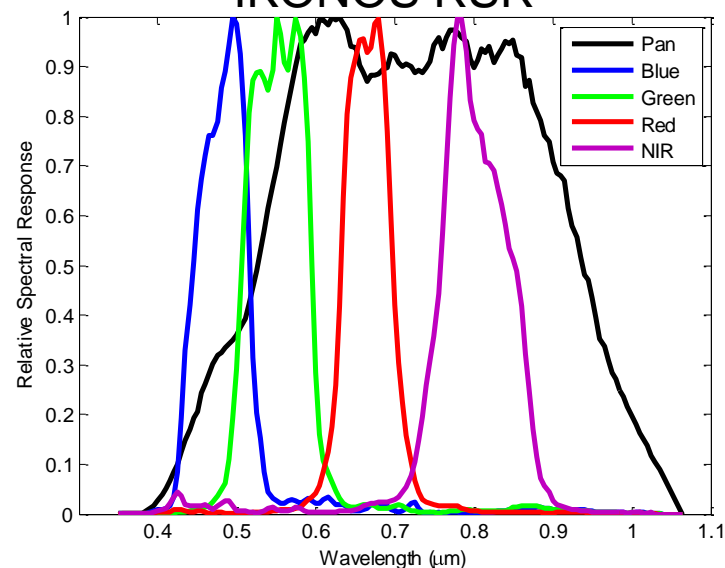
# TOA Radiance Spectrum Calculated

Apply the SPARC radiative transfer equation ,  $L_{TOA}(\lambda, \theta_r) = \rho(\lambda, \theta_r) T_1(\lambda) T_2(\lambda) E_o(\lambda) \left( \frac{R}{2GSD} \right)^2$ , and convolve the radiance ( $L_{TOA}$ ) spectrum with the sensor's relative spectral response (RSR)

Top-Of-Atmosphere Effective Radiance Spectrum For A Single Mirror



IKONOS RSR



	IKONOS TOA Band Predicted Radiance [Watts/(m2 sr micron)]			
Image/Mirror	Blue	Green	Red	NIR
po_365282 /Glass	4.128	4.345	3.919	2.817
po_365283 /Glass	4.104	4.327	3.908	2.811

Provides in-band  
radiance/mirror

Variation mainly from sensor-to-ground transmittance differences between images



# Image Analysis: Measurement of Target Signal

$$\text{Target } \Sigma \text{DN} = \sum_{n=1}^9 \left| pN(n) - \overline{DN}_{\text{background}} \right|$$

- Total Target DN summed over 3x3 window (green box).

- $\overline{DN}_{\text{background}}$  obtained from perimeter pixel average.

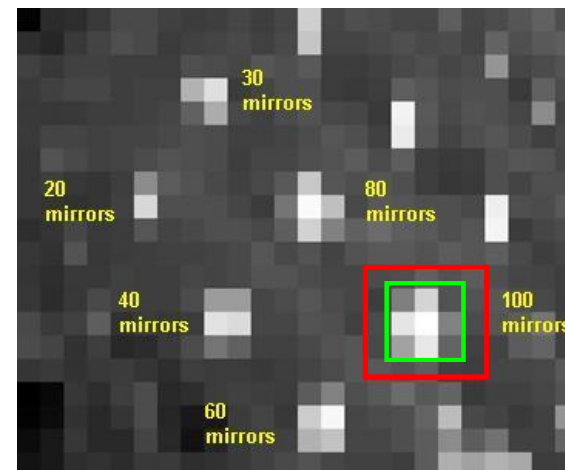
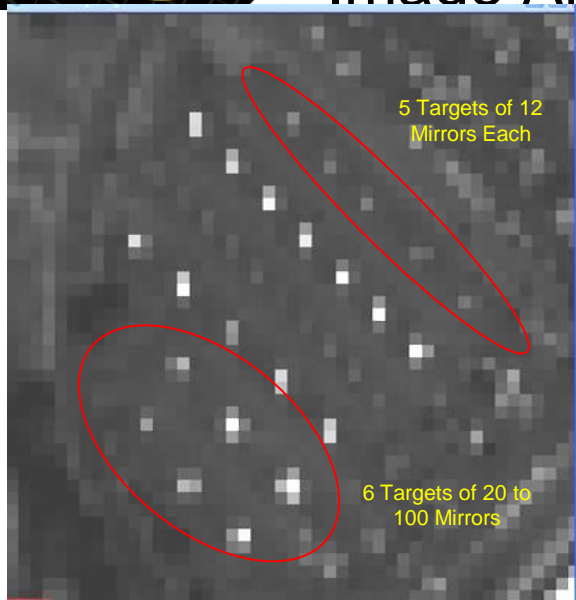
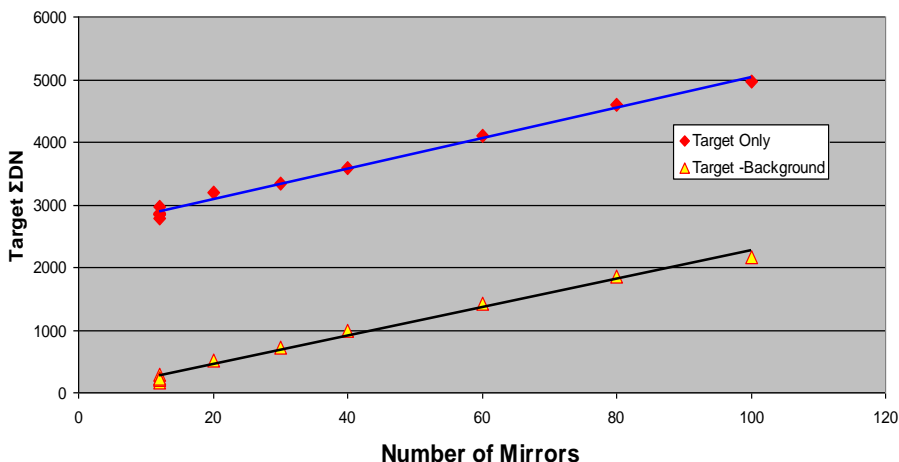


Image po\_365282 Red Band DN/Mirror



- Limited size of target area created the need for background correction (better site design would make this step unnecessary).

- Background subtraction corrects for net uniformity gradients that would introduce systematic error in slope (Example for IKONOS red band image).

Red Band Image po\_365282

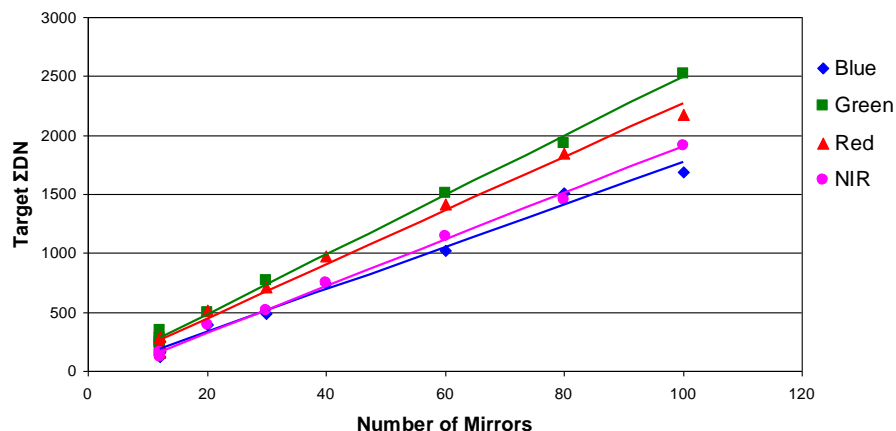
	Slope: DN/Mirror	R <sup>2</sup>	RMSE Residuals (DN)
Target Only	24.4	0.9922	67
Target - Background	22.8	0.9917	65
% Change	6.6%		

6.6 % Correction



# Image Analysis: Measurement of DN/Mirror

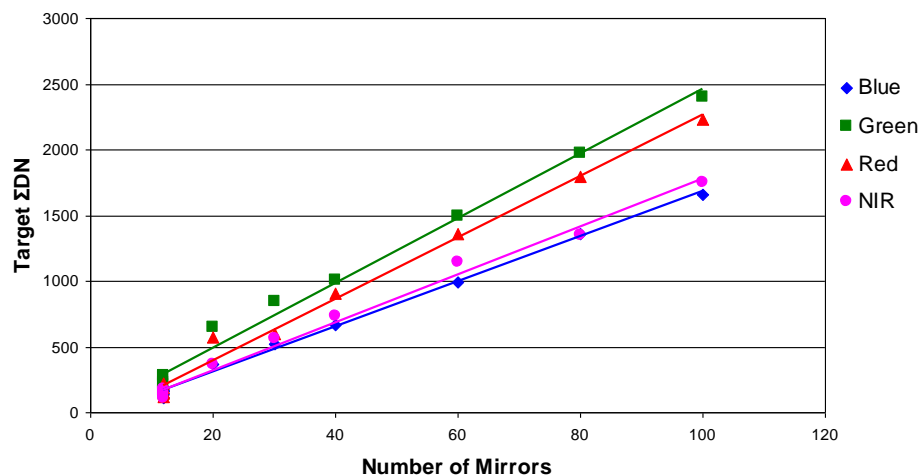
DN/Mirror: Image po\_365282 Glass Mirror SPARC Target



Spectral Band	Slope: DN/Mirror	R <sup>2</sup>
Blue	17.9	0.9898
Green	25.2	0.9972
Red	22.8	0.9917
NIR	19.8	0.9965

Slope provides the measurement of the IKONOS band responsivity

DN/Mirror: Image po\_365283 Glass Mirror SPARC Target



Spectral Band	Slope: DN/Mirror	R <sup>2</sup>
Blue	17.2	0.9963
Green	24.8	0.9886
Red	23.4	0.9904
NIR	18.2	0.9913



# IKONOS Absolute Gain Results Using the SPARC Method (Preliminary\*)

$$\text{CalCoef}(\lambda) = \frac{DN / \text{Mirror}(\lambda)}{\text{Radiance} / \text{Mirror}(\lambda) \cdot \text{Bandwidth}(\lambda) \cdot \text{EnsEnergyCor}} = DN / (\text{Watts} / \text{m}^2 \text{sr})$$

**SPARC Method Results**

	Blue	Green	Red	NIR
po_356282 / Glass Mirrors	63.1	68.1	92.6	77.8
po_365283 / Glass Mirrors	60.9	67.1	95.4	71.6
Average	62	67.6	94	74.7

**Comparison to Calibration Coefficients Provided By GeoEye.**

NASA Ground Calibration (JACIE 2001)	63.3	64.9	84	74.6
% difference	2.05	4.16	11.9	0.13
Stellar Calibration (Bowen 2001)	57.5	58	70.8	58.9
% difference	7.83	16.55	32.77	26.83

Preliminary results from the SPARC method are most consistent with reflectance-based calibration made by the NASA/JACIE team

Bandwidth from publication "IKONOS Esun Calculations" at [www.geoeye.com](http://www.geoeye.com)

\* Other 2009 collects are being processed

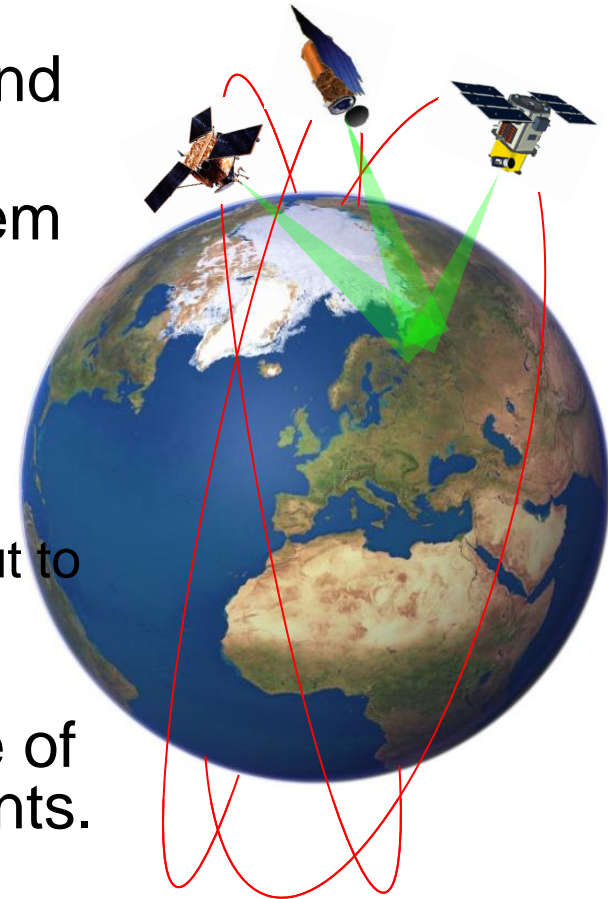


# Conclusion

- Initial results indicate that the SPARC vicarious method provides absolute calibration performance consistent with the reflectance-based vicarious calibration method.
- The SPARC method can provide simultaneous spatial and radiometric calibration.
- The SPARC method achieves absolute vicarious calibration at a significantly lower cost and effort than the reflectance-based method.
- The SPARC methodology eliminates all atmospheric effects except for transmittance in the calibration process. Potential to achieve better accuracy than reflectance-based method.
- Currently, the largest uncertainty source in deriving sensor gain comes from net gradients in target background affecting the DN/mirror measurements (Improved site design can fix this).
- Can be set up at any remote sensing study site (Does not need to be done at a high desert playa location. Validation was accomplished in a major urban setting at sea level)

# Future

- Potential to make  $<5\%$  absolute accuracy routine with a hand held sunphotometer and a few SPARC panels.
- Mountain top deployment of SPARC system could achieve  $<2\%$  absolute accuracy.
- Application to larger footprint sensors with automated pointable SPARC Panels.
- Consistent solar calibration across VNIR, SWIR, and MWIR sensors (SPARC works out to 6 microns).
- Accurate polarimetric calibration. Simply replace measured natural light reflectance of mirrors with **s** and **p** reflectance components.
- Improved cross-platform calibration of a sensor constellation. (view geometry/temporal reflectance stability with reduced atmospheric effects avoid the need for simultaneous collects)







- Acknowledgement: We would like to thank GeoEye, Inc., Thornton, Colorado, for their collaboration in providing the IKONOS imagery and specifically Martin Taylor for his fantastic job in coordinating satellite tasking with ground operations.
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